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the lectures pdfs are available at:



<https://www.physics.umd.edu/rgroups/amo/orozco/results/2022/Results22.htm>

# Correlations in Optics and Quantum Optics; A series of lectures about correlations and coherence 1. November 2022

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BOS.QT



# Lesson 2

## Tentative list of topics to cover:

- From statistics and linear algebra to power spectral densities
- Historical perspectives and examples in many areas of physics
- Correlation functions in classical optics (field-field; intensity-intensity; field-intensity)
- Correlation functions in quantum examples
- Correlations and conditional dynamics for control
- Correlations in quantum optics of the field and intensity
- Optical Cavity QED
- From Cavity QED to waveguide QED.

History

- Auguste Bravais (1811-63), French, physicist, also worked on meteorology.
- Francis Galton (1822-1911), English, statistician, sociologist, psychologist, proto-geneticist, eugenicist.
- Norbert Wiener (1894-1964), United States, mathematician interested in noise.

# Correlations for filtering



## A data filter.

- If the signal is known: take the data vector  $x_j$  with length  $m$  calculate the internal product with the signal vector  $s_i$  of length  $n$ , with  $n < m$
- Start with  $i=j=0$  until  $i=n$  y  $j=n$  and get  $C_0$
- Move the signal vector over the data by one unit  $i=0$   $j=1$  until  $i=n$  y  $j=n+1$  obtaining  $C_1$ , continue this way until you reach  $C_m$
- $C(m)$  will be maximal when the signal and the data coincide. The noise will average down to zero.

These filters can be calculated from basic principles of based on measurements.

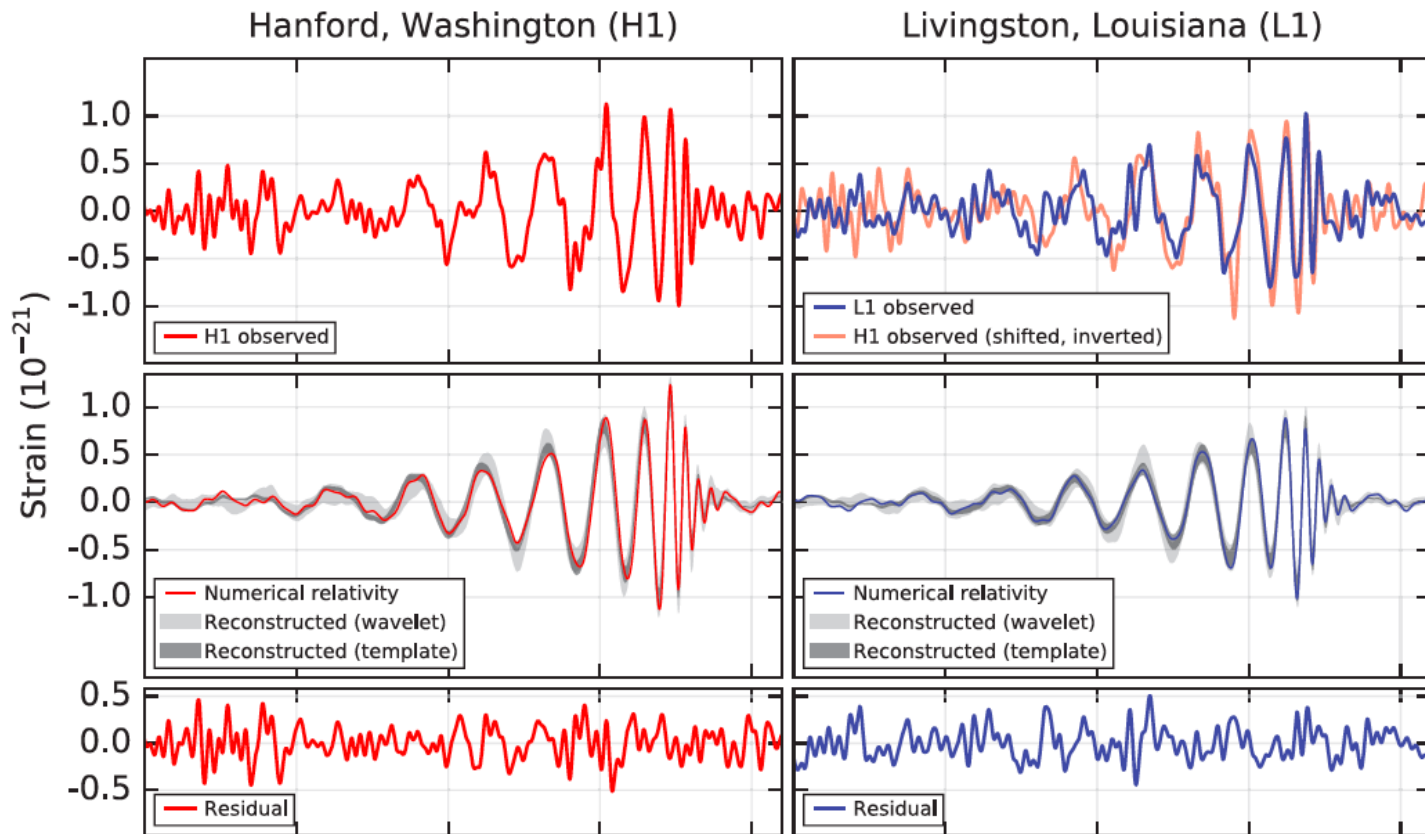
Examples:

LIGO

Modern hearing aids

The Wiener–Khinchin-Kolmogorov theorem allows the us to use the power spectral density to calculate the correlation, this is much more effective numerically ( $n \ln(n)$ ) instead of  $n^2$

# LIGO used correlations to find gravitational waves.



The original experiment of Hanbury  
Brown, Jennison, and Das Gupta

## APPARENT ANGULAR SIZES OF DISCRETE RADIO SOURCES

### Observations at Jodrell Bank, Manchester

THE existence of discrete sources of extra-terrestrial radio-frequency radiation is now well established<sup>1,2</sup> and the positions of more than one hundred sources have been published<sup>3-5</sup>. Attempts to identify these sources with any particular class of visual object have so far failed, and the origin of the radiation remains unexplained. One of the fundamental requirements in the study of these sources is a knowledge of their apparent angular size, and although attempts to make this measurement have been made by several observers<sup>1-3</sup>, it has proved to be beyond the resolving power of their equipment. The present communication gives a preliminary account of a successful attempt to measure the angular size of the two most intense sources the positions<sup>6</sup> and intensities<sup>4</sup> of which are given in Table 1.

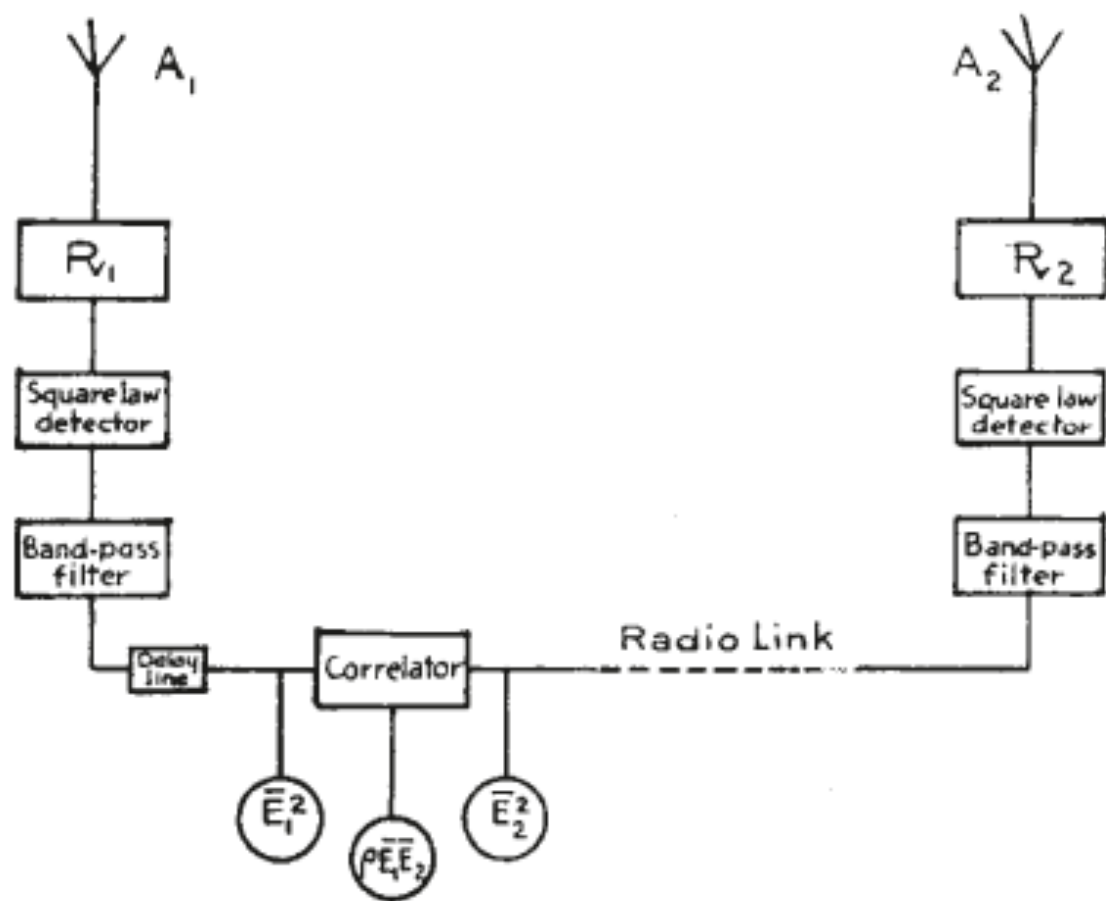
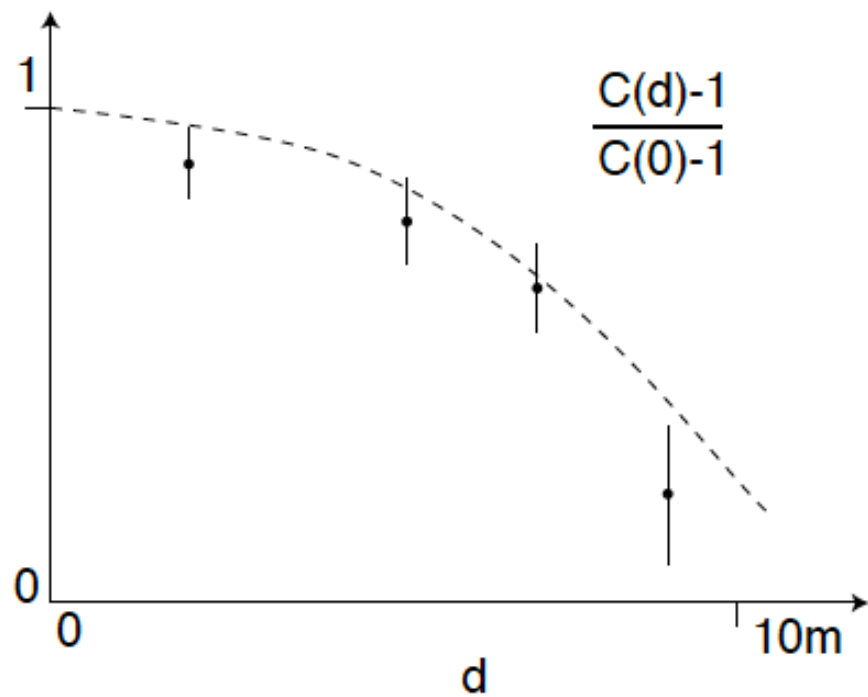


Fig. 1. Schematic diagram of the equipment

Table 2. EXPERIMENTAL RESULTS

Base-line		Cygnus		Cassiopeia	
Length* (km.)	Bearing†	Correlation coefficient	Angular width of equivalent strip	Correlation coefficient	Angular width of equivalent strip
<i>A</i> 0.30	349.5°	0.99 ± 0.10	< 5'	0.96 ± 0.09	3' 40" (< 5' 50")
<i>B</i> 2.16	113.0°	0.30 ± 0.03	2' 10" ± 4"	0.08 ± 0.02	2' 55" ± 10"
<i>C</i> 2.16	235.5°	0.79 ± 0.08	1' 00" ± 7"	< 0.01	✶ 3' 30"
<i>D</i> 3.99	177.0°	0.79 ± 0.07	0' 34" ± 8"	0.07 ± 0.01**	



Measurement of the angular diameter of Sirius [15].



# Correlations in particle physics

**PION-PION CORRELATIONS IN ANTIPROTON ANNIHILATION EVENTS\***

Gerson Goldhaber, William B. Fowler, Sulamith Goldhaber, T. F. Hoang,  
Theodore E. Kalogeropoulos, and Wilson M. Powell

Lawrence Radiation Laboratory and Department of Physics, University of California, Berkeley, California

(Received July 17, 1959)

We have observed angular correlation effects between pions emitted from antiproton annihilation events. This experiment was carried out with a separated antiproton beam<sup>1</sup> of momentum  $p_{\bar{p}}$  = 1.05 Bev/c. A total of 2500 annihilation events were observed in 20 000 pictures taken with the Lawrence Radiation Laboratory 30-in. propane bubble chamber.

$$\cos\theta_{12} = \vec{p}_1 \cdot \vec{p}_2 / |p_1| |p_2|.$$

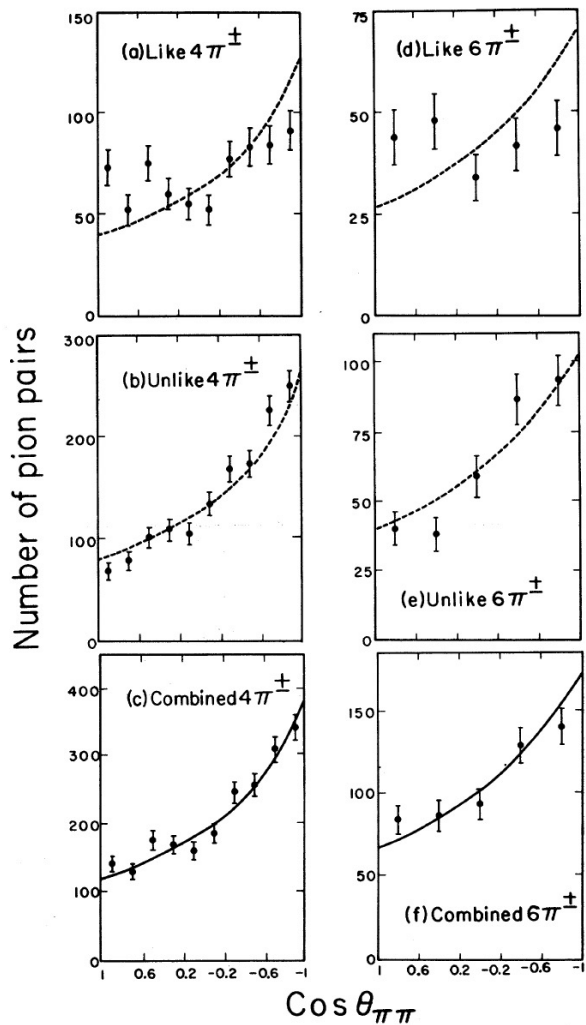


FIG. 1. Distribution of angles between pion pairs as a function of  $\cos\theta_{\pi\pi}$ . The curves correspond to

This is the way they now  
measure the size of the  
quark-gluon plasma

The physics of Hanbury Brown–Twiss intensity  
interferometry: from stars to nuclear collisions  
Gordon Baym, *Acta Phys. Polon. B29* 1839,(1998)

[arXiv:nuc-th/9804026](https://arxiv.org/abs/nuc-th/9804026)

# Astrophysics

Arno Penzias and Robert Wilson from Bell Labs discovered the remnants of the Big Bang in 1965. Trying to understand some noise [Cosmic Microwave Background].

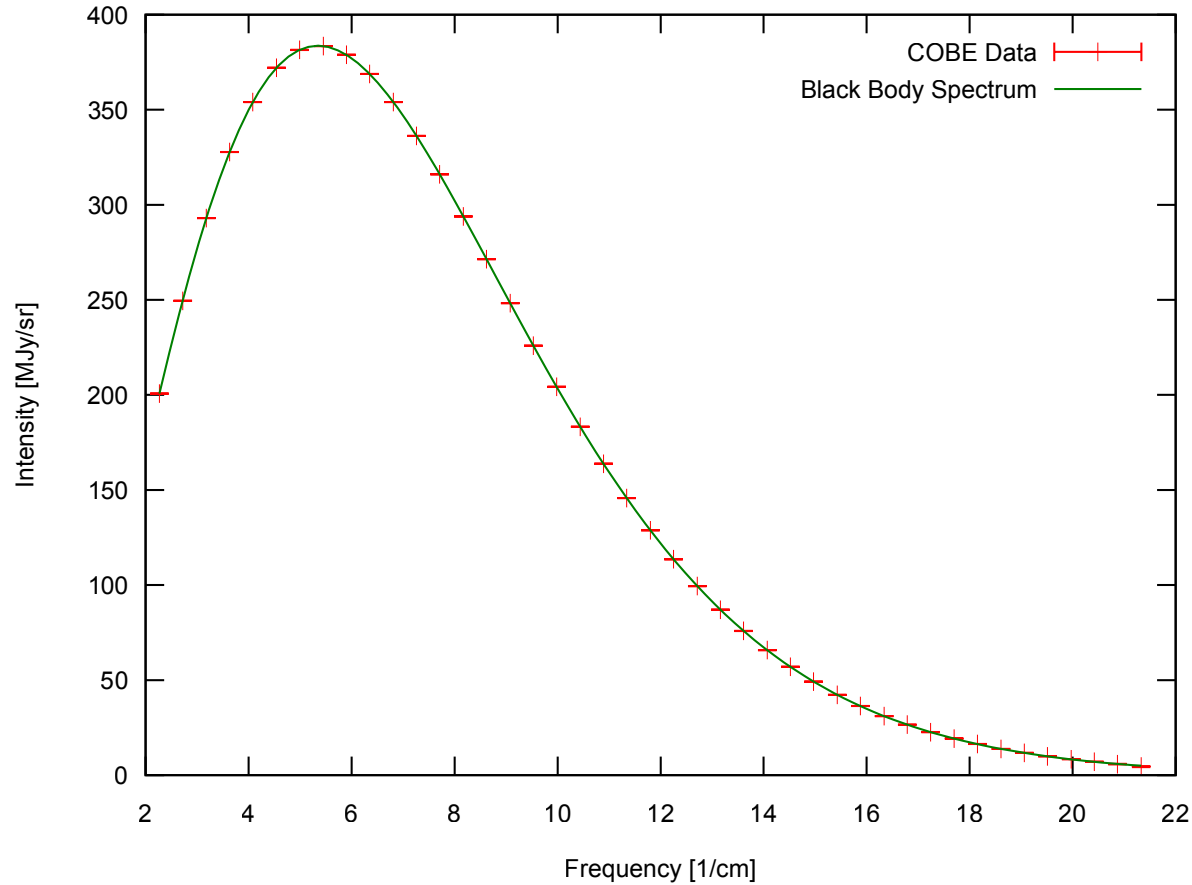


How is the CMB generated?

379,000 after the Big Bang, the universe has cooled enough to form neutral atoms and the majority of the radiation can now escape.

This radiation is almost uniform but has very small fluctuations ( $\partial T/T \sim 10^{-6}$ ) which come from quantum fluctuations. Gravity plays a very important role. The fluctuations are the seeds for the formation of galaxies, etc.

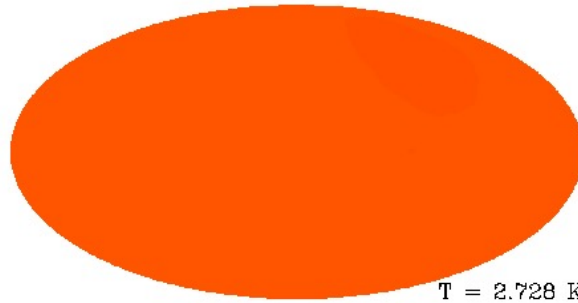
Cosmic Microwave Background Spectrum from COBE



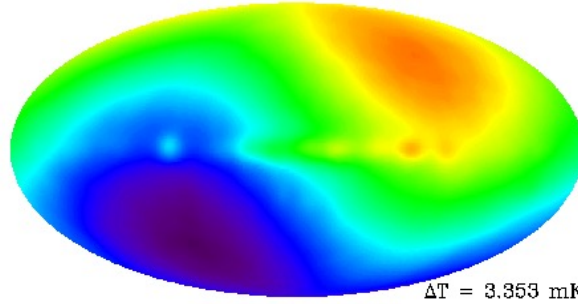
(CMB) John Mather and Gary Hinshaw Scientific Directors



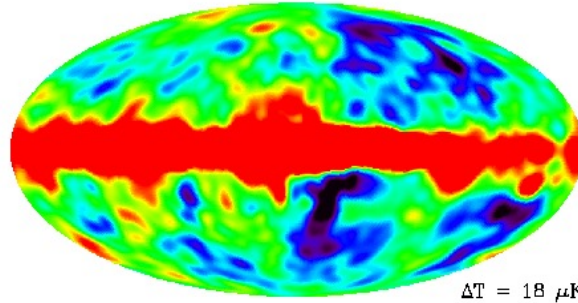
COBE 1992



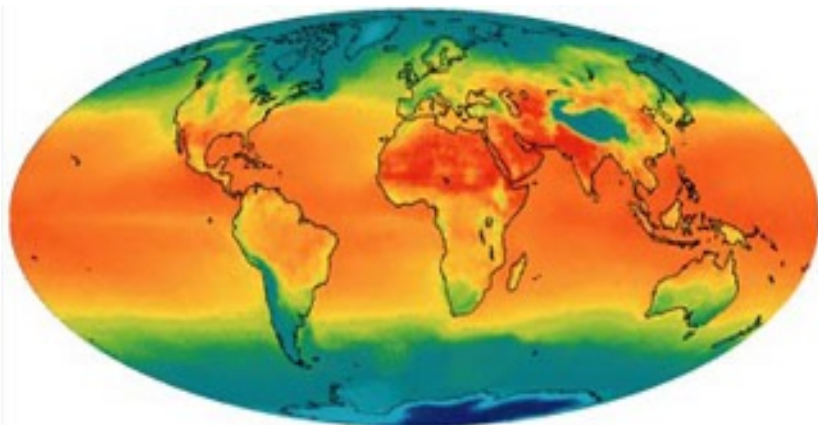
Measurement



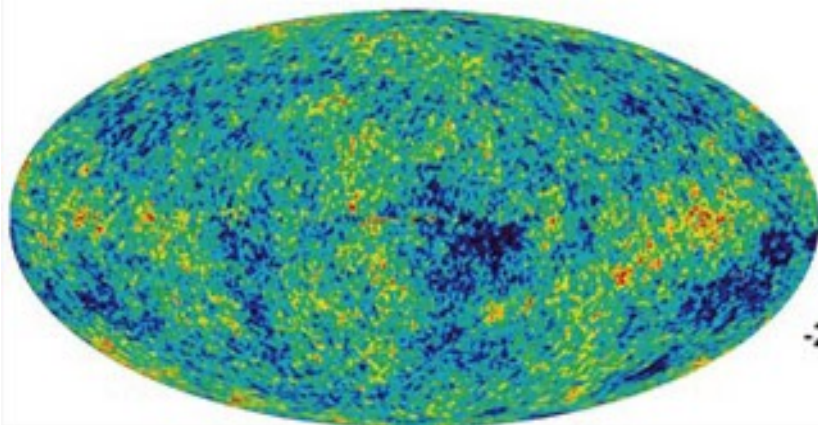
Dipole,  
from  
moving



Remaining  
Fluctuations



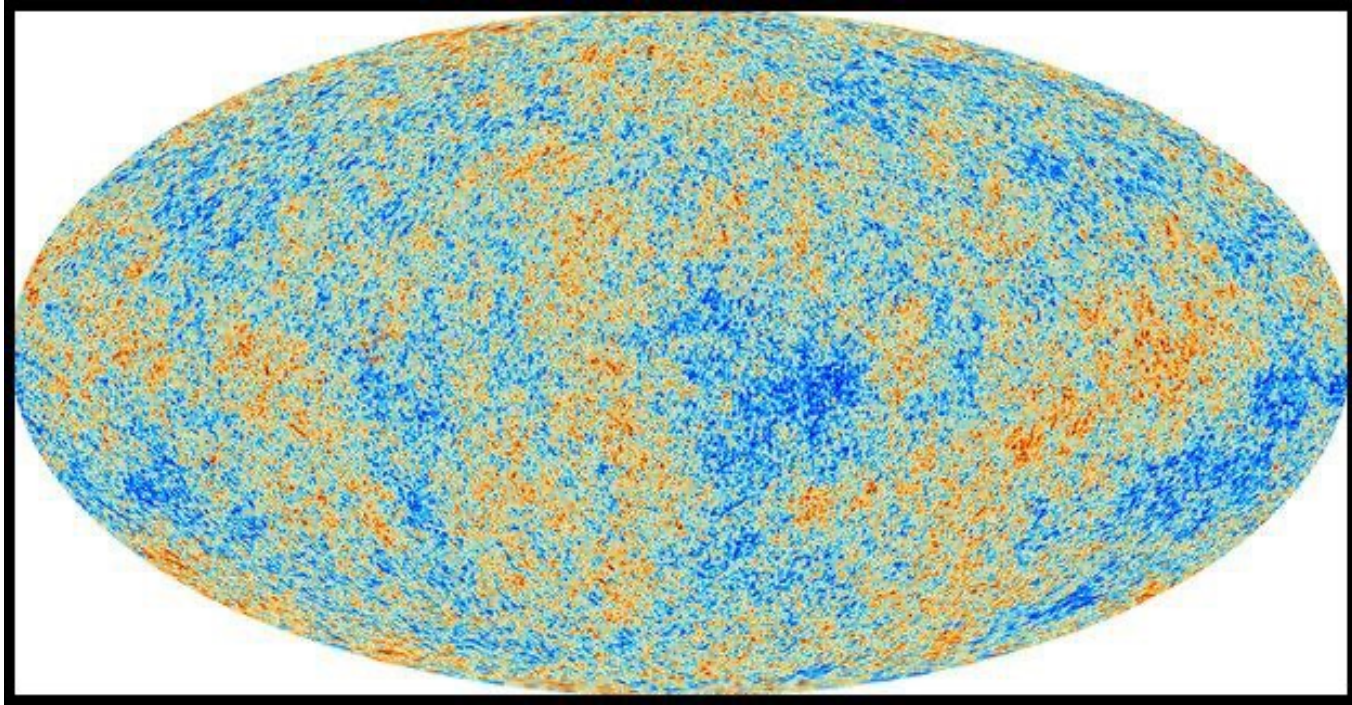
Earth  
Temperatures



Microwave Sky  
Temperatures

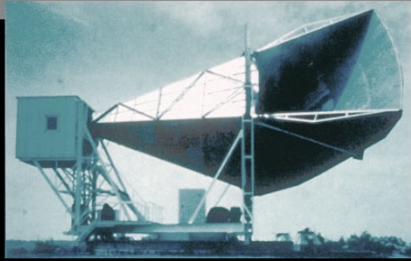


# Results from Planck 2013

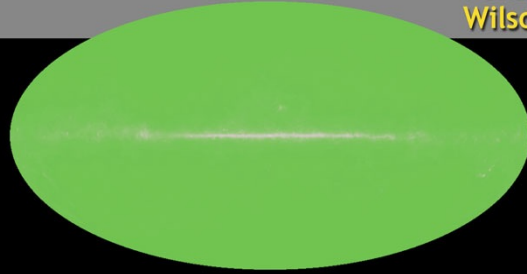


Some 379,000 years after the Big Bang

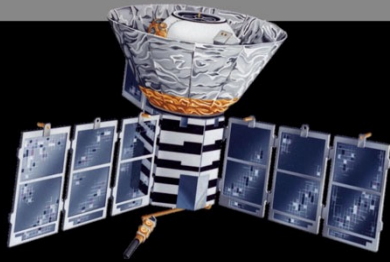
1965



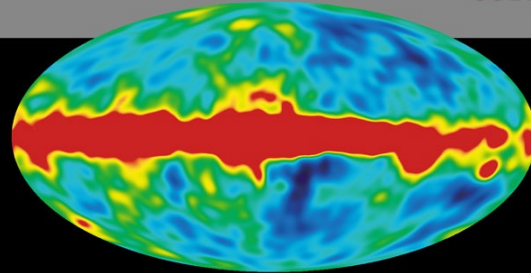
Penzias and  
Wilson



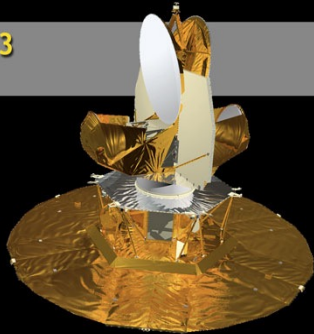
1992



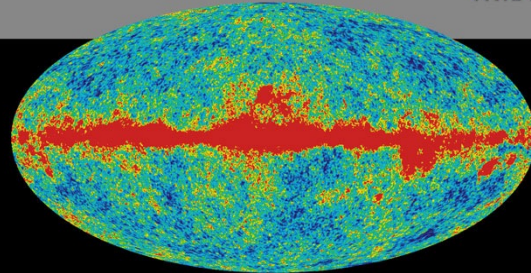
COBE



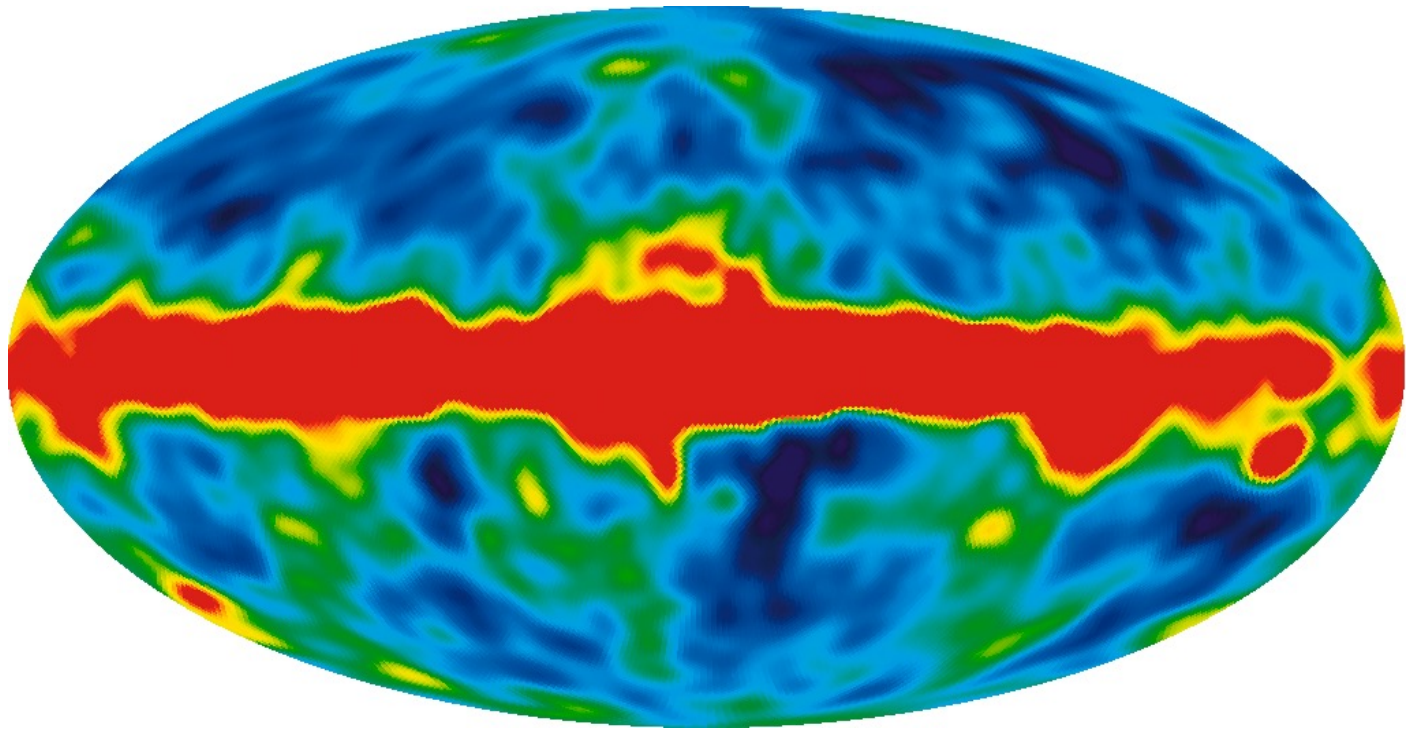
2003



WMAP

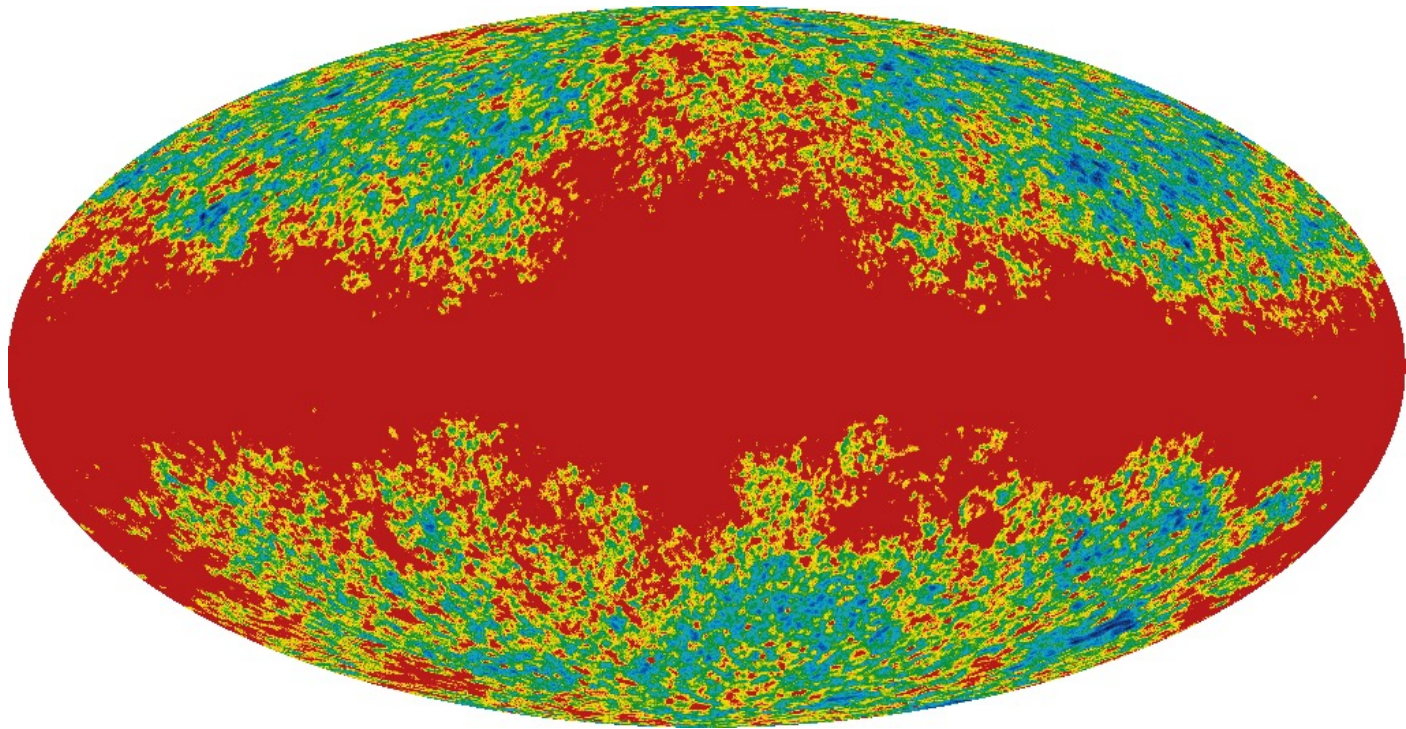




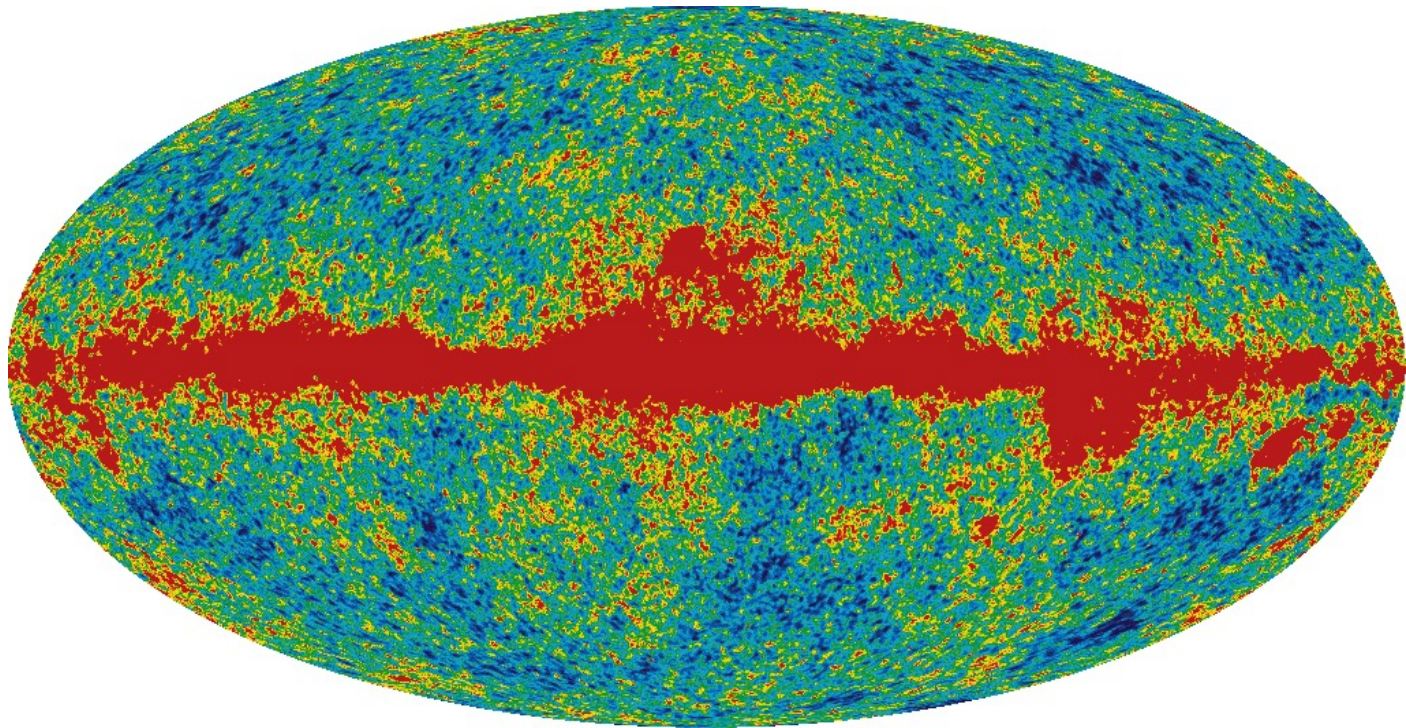


COBE launched in 1989 4 year result: resolution 7  
degrees and 100  $\mu$ -Kelvin.

2006 Nobel for George Smoot and John Mather

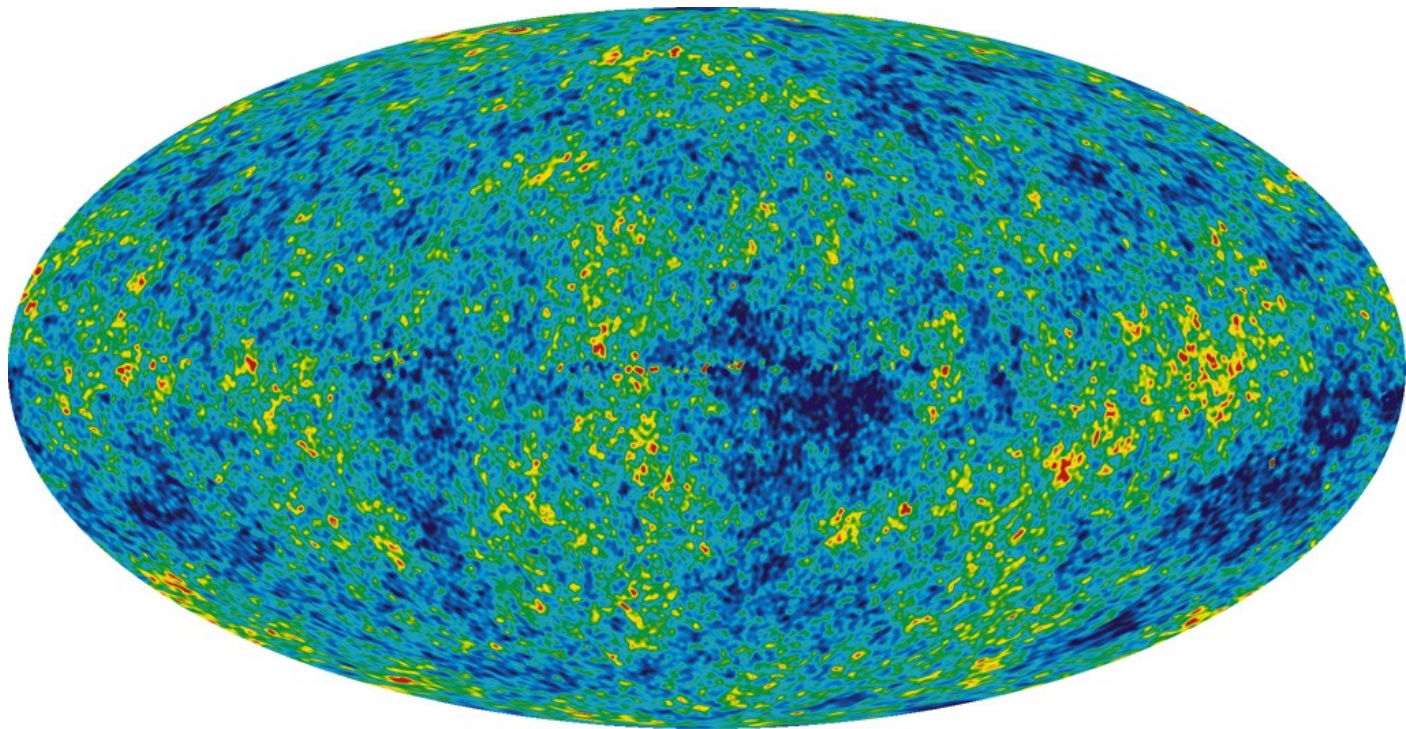


5 years WMAP band K (20 to 30 GHz)



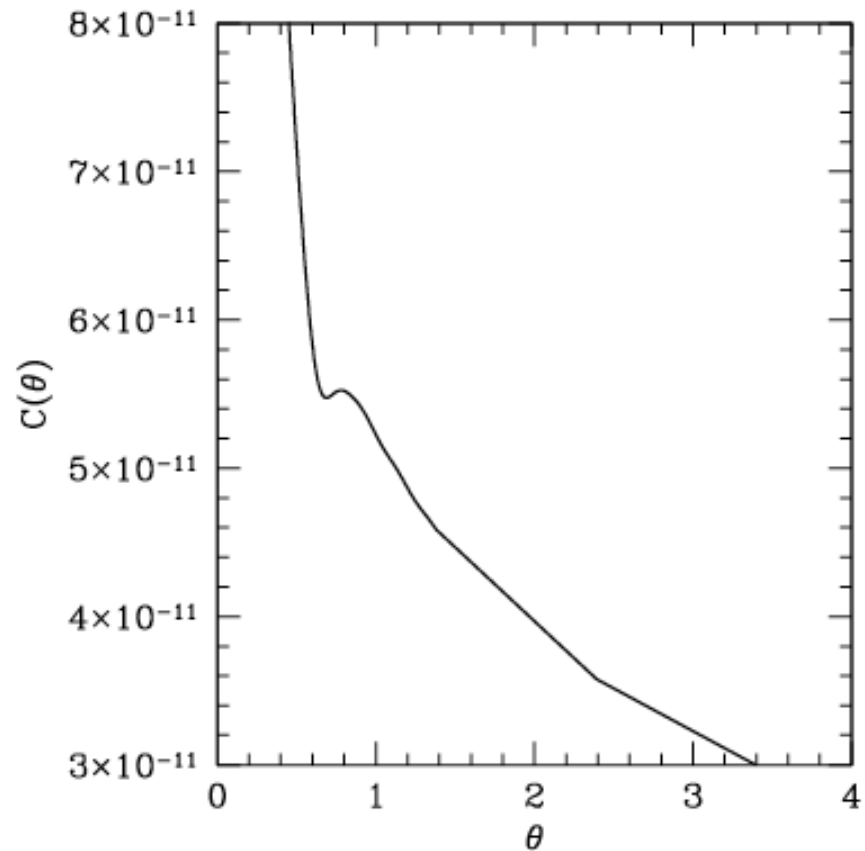
Band Q 33 to 50 GHz (6 mm)



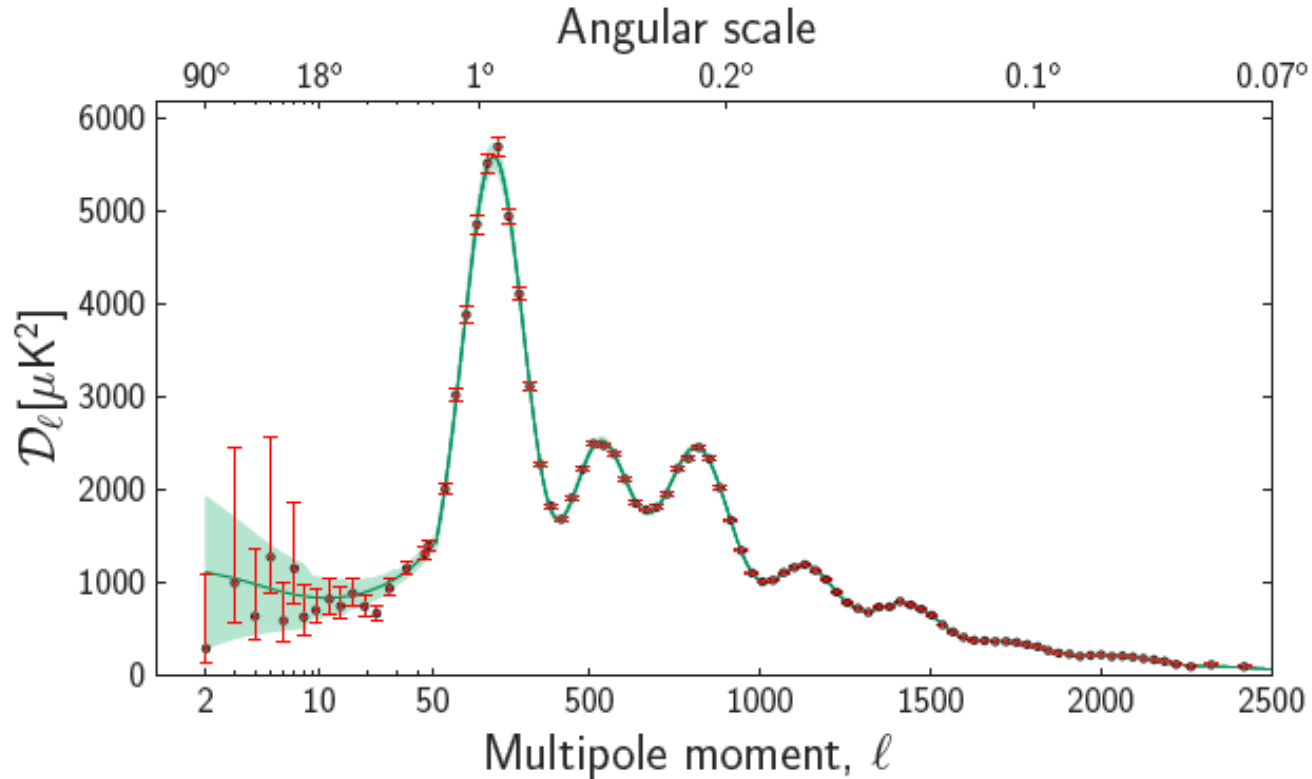


Fluctuations on the WMAP  
5 years (subtracting the milky way) 200  $\mu$ -Kelvin





Correlation function of the fluctuations on the CMB showing the acoustic sound horizon. ArXive 1506.01907



Power spectrum (Planck) of the fluctuations in CMB as a function of multipole moment  $l$  and angle. ArXive 1506.01907, James Peebles Nobel Prize 2019

What do those  
fluctuations tell us?

- The matter distribution was very uniform in the early universe, but it had to have fluctuations to generate the structures that we see Today (galaxies, etc.)
- These fluctuations in the density affected the temperature of the emitted photons in each region: In a dense region, the photons had to overcome a larger gravitational potential, so they should have acquired a larger red shift cooling them.

Later oscillations (acoustic sound horizon) are not possible with the existing baryonic matter. They are related with non baryonic dark matter.

Thanks